



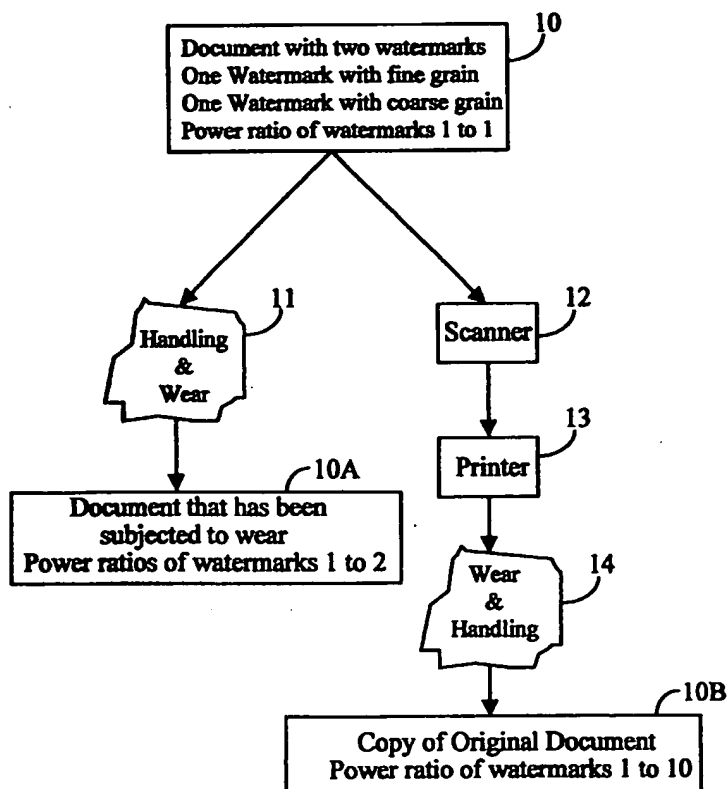
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(54) Title: **MULTIPLE WATERMARKING TECHNIQUES**

(57) Abstract

Multiple digital watermarks, each of which has different characteristics, are embedded in a document. The characteristics of the various watermarks are chosen so that each of the watermarks will be affected in a different manner if the document is subsequently copied and reproduced. The detection process or mechanism reads each of the watermarks and compares their characteristics. While wear and handling may change the characteristics of the digital watermarks in a document, the relationship between the characteristic of multiple digital watermarks in a document will nevertheless give an indication as to whether a document is an original or a copy of an original.



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MULTIPLE WATERMARKING TECHNIQUES**Field of the Invention:**

The present invention relates to steganography and more particularly to the use of watermarks to determine the authenticity and history of a particular document or image.

Background of the Invention:

Steganographic and digital watermarking technologies are well known. For example see U.S. Patent 5,636,292 and the extensive references cited therein. Also see copending patent applications serial number 08/327,426 which was filed 10/21/94 and copending application serial number 08/436,134 which was filed 5/8/95.

The technology for inserting digital watermarks in images and the technology for reading or detecting digital watermarks in images is well developed, well known and described in detail in public literature. Furthermore, there are commercially available products which include programs or mechanisms for inserting digital watermarks into images. For example the commercially available and widely used products "Adobe Photoshop" which is marketed by Adobe Corporation of San Jose California and "Corel Draw" program which is marketed by Corel Corporation of Ontario Canada, include a facility for inserting digital watermarks into images.

The technology for making high quality copies of documents is widely available. The technical quality of scanners and color printers has been increasing rapidly. Today for a relatively low cost one can purchase a high quality scanner and a high quality color printer. Thus, it is becoming increasingly easy to duplicate documents. The ability to create high quality copies has created a need for technology which can differentiate between original documents and copies of the original.

1
2 It is known that watermarks can be used to help differentiate genuine documents
3 from copies. However, the prior art techniques for using digital watermarks to
4 differentiate genuine documents from copies have serious limitations. The present
5 invention is directed to an improved technique for using steganography and digital
6 watermark technology to facilitate differentiating original documents from copies of
7 the original.

8
9 The present invention can also be used for various other purposes such as to
10 embed multiple types of information in a single document or to provide watermarks
11 which enable documents to perform special functions.

12
13 **Summary of the Invention:**

14 With the present invention multiple digital watermarks, each of which has different
15 characteristics are embedded in a document. The characteristics of the two
16 watermarks are chosen so that each of the watermarks will be affected in a different
17 manner by what may subsequently happen to the document.

18
19 The detection process or mechanism reads the two digital watermarks and
20 compares their characteristics. While wear and handling may change the
21 characteristics of the individual watermarks, the relationship between the
22 characteristic of the two watermarks will never-the-less give an indication as to
23 whether a document is an original or a copy of an original.

24
25 For example according to the present invention two digital watermarks in a
26 document may have different energy levels. The absolute energy level of a digital
27 watermark in an original image may be decreased if a document is subject to wear.

1 Likewise the energy level of the digital watermark in an image may be decreased if
2 an image is scanned and reprinted on a color printer. However, the relationship
3 between the energy level of the two digital watermarks will be different in an image
4 that has been subject to wear and in a reproduced image. Likewise if two digital
5 watermarks are introduced into an image where the bit pattern used to construct the
6 digital watermarks have different patterns, the ratio between the signal to noise ratio
7 of the watermarks will be different in an original subject to wear and in a copy
8 generated by scanning the original and printing the scanned image. Other
9 characteristics of multiple digital watermarks can also be used to differentiate
10 original documents from copies.

11

12 **Brief Description of the Figures:**

13 Figure 1 shows the paths that a document and a copy may follow.

14 Figures 2A and 2B show a fine grain and a course grain watermark.

15 Figure 3A and 3B show a geometrically linear and a geometrically random

16 assignment of pixels to a bit in a digital watermark.

17 Figure 4 illustrates a fourth embodiment of the invention.

18

19 **Detailed Description of preferred embodiments:**

20 The problem of differentiating an original document from a copy is made more
21 difficult in situations where the original document is subject to being handled, worn,
22 folded and otherwise damaged. Many original documents such as identification
23 documents and currency are extensively handled. The wear to which such
24 documents are subjected reduces the quality of images on the document and
25 therefore reduces the quality of any information embedded in the document using
26 conventional steganographic techniques.

27

1 With the present invention a number of different watermarks are embedded in a
2 document. Each of the watermarks embedded in the document, has different
3 characteristics. All watermarks are somewhat affected when a document is
4 subjected to wear, and all watermarks are somewhat affected when a document is
5 duplicated by being scanned and reprinted. However, the magnitude of the effect
6 caused by being scanned and reprinted on watermarks with certain characteristics
7 is much greater than the effect on watermarks with different characteristics.

8 Likewise, wear and handling of a document affects watermarks with certain
9 characteristics much more than it affects watermarks with different characteristics.

10

11 Thus, if multiple watermarks with different characteristics are inserted into a
12 document, it is possible to differentiate a copy from an original document that has
13 been subjected to wear by examining the ratios of characteristics of the watermarks
14 in the image being examined.

15

16 In order to print a document on a color printer, the document is put through a
17 transformation from a color space such as the RGB color space to a different color
18 space such as the CMYK (cyan, magenta, yellow, black) color space. Such
19 transformations are well know. For example see chapter 3 entitled "Color Spaces"
20 in a book entitled "Video Demystified, A handbook for the Digital Engineer", Second
21 Edition, by Keith Jack, published by Harris Semiconductor and Hightext Publications
22 of San Diego, California.

23

24 When an image is transformed from one color space to another color space, noise
25 is introduced into the image. Among the reasons for this is the fact that each color
26 space has its own distinctive gamut (or range) of colors. Where the gamut of two
27 color spaces overlap, the conversion from one color space to another color space

1 can in theory be precise. However, there will be some areas which are in the gamut
2 of one color space not in the gamut of another color space. Such situations
3 definitely introduce noise into the conversion process. Even in areas that are in the
4 gamut of two color spaces, conversion from one color space to another color space
5 introduces noise because of such things as round off errors. The present invention
6 takes advantage of the fact that if an original is copied and then a copy is printed,
7 the image on the printed copy will have gone through several conversions to which
8 the original will not have been subjected. For example, the conversions to which a
9 copy may be subjected

10 are:

- 11 1) a document to RGB conversion (i.e. scanning the document into the computer),
- 12 2) a RGB to CMYK conversion,
- 13 3) a CMYK to copy conversion (i.e. printing the document).

14 Any characteristics of the two digital watermarks that will be affected differently by
15 the additional conversion process to which copies are subjected can be used to
16 differentiate copies from an original. Since the two watermarks with different
17 characteristics are affected in a different manner by the additional conversion step,
18 a comparison of the characteristics of the two watermarks in a document being
19 examined will indicate if the document is an original (which has not gone through
20 the additional conversions) or a copy which has gone through the additional
21 conversions. While the characteristics of each watermark will have been changed
22 by wear and by the copying process, the comparison between the characteristics of
23 the two watermarks will still be able to differential a copy from an original.

24

25 Four embodiments of the invention are described below. Each of the embodiments
26 utilizes two watermarks in a document. The differences between the two
27 watermarks in the document are as follows:

1 In the first embodiment:

2 First watermark: Has fine grain

3 Second watermark: Has a course grain

4 In the second embodiment:

5 First watermark: Has geometrically linear assignment of pixels

6 Second watermark: Has geometrically random assignment of pixels.

7 In the third embodiment:

8 First watermark: Has low power

9 Second watermark: Has higher power

10 In the fourth embodiment:

11 First watermark: uses standard RGB to HSI and HSI to RGB transformations

12 Second watermark is biased before being transformed from HSI to RGB.

13

14 Figure 1 shows the steps to which documents and copies are typically subjected. In

15 the normal course, a document 10 may be subjected to handling and wear 11

16 resulting in a worn document 10A. Document 10 may also be scanned as illustrated

17 by box 12. The scanning produces a digital image which can be printed as

18 illustrated by box 13. The printed image may be subjected to handling and wear 14

19 resulting in a copy 10B. It is noted that the document 10 may also be subject to

20 handling and wear prior to the scanning operation 12. The task to which this

21 invention is directed is the task of differentiating the worn document 10A from the

22 copy 10B.

23

24 The document 10 includes an image (not explicitly shown) which has two digital

25 watermarks inserted therein. In the first embodiment of the invention, the first

26 watermark has a fine grain and the second watermark has a course grain. The

27 grain of the two watermarks is illustrated in Figure 2. Figure 2A shows the grain of

1 the first watermark and figure 2B shows the grain of the second watermark. The
2 first watermark uses blocks of 9 pixels (a 3 by 3 block). Each of the pixels in each 9
3 pixel block has its gray value changed by the same amount. For example Figure 2A
4 shows that the first 9 pixel block has its gray value increase and the second 9 pixel
5 block has its gray value decreased. The amount of increase and the selection of
6 blocks that is increased and decreased is conventional.

7
8 As shown in Figure 2B, the grain of the second watermark is in blocks that are 6
9 pixels by 6 pixels or 36 pixels. All of the pixels in each 36 pixel block are changed
10 by the same amount.

11
12 In the original document 10, the two watermarks have a power ratios of 1 to 1. After
13 wear and handling, the power of the first watermark will be degraded somewhat
14 more than the power of the second watermark. For example, as illustrated in Figure
15 1, after document 10 is subjected to handling and wear, a detector which reads the
16 watermarks might find that the power ratio of the water marks is 1 to 2.

17
18 If the document 10 is scanned and the resulting digital image is printed to make a
19 copy of the document 10, the ratio of the power of the watermarks will be affected
20 much more than the effect of handling and wear. For example as illustrated in
21 Figure 1, the power ratio of the watermarks may be 1 to 10, thereby allowing one to
22 differentiate the worn original document 10A from the copy 10B.

23
24 It is noted that the mechanism for inserting watermarks into an image is well known
25 as is the technique for reading a watermark and using correlation techniques to
26 determine the signal to noise ratio (i.e. the power) of a watermark.

1 Figures 3A and 3B shown an alternative technique for implementing the present
2 invention. In the second embodiment of the invention, the two watermarks inserted
3 into the image on a document have different patterns of assigning pixels to the bits
4 of the number which the watermark represents. The first watermark utilizes a
5 geometrically linear assignment of pixels to each bit. For example Figure 3A shows
6 an image that has 500 by 500 pixels. Considering a watermark with 50 bits, each
7 bit of the watermark would have 5000 pixels assigned to represent that bit. A linear
8 assignment could have each fifth bit in each row (100 bits per row) and each fifth
9 row (50 rows) assigned to each bit of the watermark. Thus 5000 pixels would be
10 assigned to each bit in a very orderly or linear manner.

11
12 In the second watermark the pixels would be assigned to each bit in a random
13 manner as shown in Figure 3B. Each bit in the watermark would still have 5000
14 assigned bits; however, the pixels would be a random location over the image.
15 Naturally it should be understood that Figure 3A and 3B illustrate how pixels are
16 assigned to one bit of the watermark. The other bits of the watermarks would have
17 pixels assigned in a similar manner.

18
19 Similar to the first embodiment of the invention, the watermark with a linear
20 assignment of pixels and the watermark with a random assignment of pixels would
21 be affected differently by handling and wear on the original document than they
22 would be by being scanned and reprinted.

23
24 The third embodiment of the invention described herein utilizes watermarks which
25 have different power levels. Handling and wear as contrasted to scanning and
26 printing would affect a watermark with a low power level differently than a water
27 mark with a high power level. Watermarks with different power levels can be

1 inserted into a document in order to practice the present invention utilizing
2 commercially available programs such as Adobe Photoshop or Corel Draw. In the
3 Adobe Photoshop and Corel Draw programs, the power or intensity of the
4 watermark can be adjusted by setting a simple control setting in the program.

5

6 The fourth embodiment of the invention introduces different characteristics into two
7 watermarks by modifications made to one of the watermarks during the initial step
8 during which the watermarks are introduced into an image. The operation of the
9 fourth embodiment can be explained as shown in Figure 4. First as illustrated by
10 equation 1 there is a conversion from RGB to HSI as is conventional. This is
11 illustrated by equation 1. As illustrated by equation 2, the first watermark is inserted
12 into the image in a conventional manner by modifying the I value in the HSI
13 representation of the image using the first watermark values (designated as WM1
14 Δ). A first RGB value designated RGB(1) is then calculated using a conventional
15 transformation designated T. As indicated by equation 3, the second watermark
16 WM2 is then biased toward a particular color and the biased watermark is then
17 combined with the HSI values and transformed to a second set of RGB values
18 designated RGB(2). Finally as indicated by equation 4, the values RGB(1) and
19 RGB(2) are combined to form the watermarked image designated RGB(F).

20

21 The transform used to go from RGB to HSI color space (indicated in equation 1 in
22 Figure 4) can be anyone of a variety of known other techniques. For example, the
23 RGB to HSI conversion can be one of the techniques explained in the above
24 referenced text book such as the following: (which assumes that RGB and Intensity
25 have a value range of 0 to 1 and that Red equals 0°):

26 First calculate:

27 $M = \max (R,G,B)$

$$1 \quad m = \min (R, G, B)$$

$$2 \quad r = (M-R)/(M-m)$$

$$3 \quad g = (M-G) / (M-m)$$

$$4 \quad b = (M-B) / (M-m)$$

5 Then calculate I, S, and H as follows:

$$6 \quad a) \quad I = (M + m) / 2$$

$$7 \quad b) \quad \text{if } M = m \text{ then } S = 0 \text{ and } H = 180$$

$$8 \quad \text{if } I < \text{or } = 0.5 \text{ then } S = (M-m)/(M+m)$$

$$9 \quad \text{if } I > 0.5 \text{ then } S = (M-m) / (2-M-m)$$

$$10 \quad c) \quad \text{if } R = M \text{ then } H = 60 (b-g)$$

$$11 \quad \text{if } G = M \text{ then } H = 60 (2 + r - b)$$

$$12 \quad \text{if } B = M \text{ then } H = 60(4 + g - r)$$

$$13 \quad \text{if } H > \text{or } = 360 \text{ then } H = H - 360$$

$$14 \quad \text{if } H < 0 \text{ then } H = H + 360$$

15 The first watermark is inserted into the RGB values in a conventional manner by
 16 modifying the I value of appropriate pixels so as to combine the watermark Δ values
 17 with HSI values. This is indicated by equation 2 in Figure 4. Next as indicated by
 18 equation 3 in Figure 4, the HSI values are converted to RGB values using a
 19 transform "T". The transform "T" can be conventional and it can for example be
 20 done as follows:

21 First calculate:

$$22 \quad \text{if } I < \text{or } = 0.5 \text{ then } M = I (1 + S)$$

$$23 \quad \text{if } I > 0.5 \text{ then } M = I + S - IS$$

$$24 \quad m = 2I - M$$

$$25 \quad \text{if } S = 0 \text{ then } R = G = B = I \text{ and } H = 180^\circ$$

26 Then calculate R, G and B as follows:

$$27 \quad a) \quad \text{if } H < 60 \text{ then } R = M$$

1 if $H < 120$ then $R = m + ((M-m) / ((120- H) / 60))$

2 if $H < 240$ then $R = m$

3 if $H < 300$ then $R = m + ((M - m) / ((H - 240 / 60))$

4 otherwise $R = M$

5

6 b) if $H < 60$ then $G = m + ((M-m) / (H/60))$

7 if $H < 180$ then $G = M$

8 if $H < 240$ then $G = m + ((M - m) / ((240 - H_ / 60))$

9 otherwise $G = m$

10 c) if $H < 120$ then $B = m$

11 if $H < 180$ then $B = m + ((M - m) / ((H-120/60))$

12 if $H < 300$ then $B = M$

13 otherwise $B = m + ((M - m) / ((360 - H) / 60))$

14

15 Next the values which represent a second watermark are used to calculate a

16 second set of RGB values designated RGB2. In order to calculate RGB2, the

17 values of H and S are modified so that they are slightly biased toward a particular

18 color designated H1 and S1. New values for H and S are calculated as follows:

19 (Note, H1 must be between 0 and 360, S1 must be non-negative and can be

20 between 0 and 1 and X is a value between 0 and 1)

21 Calculate new values for H and S as follows:

22 If $H > H1$ then $H = H - (H - H1) \times$

23 else $H = H + (H1 - H) \times$

24 If $S > S1$ then $S = S - (S - S1) \times$

25 else $S = S + (S1 - S) \times$

26 :

1 Next add the second watermark to the values of HSI and transform these values to
2 the RGB color space as indicated by equation 3. The transformation from HSI color
3 space to RGB color space is done as previously indicated.

4

5 Finally as indicated by equation 4 in Figure 4, the final RGB value (designated
6 RGBF) is calculated by combining the values of RGB1 and RGB2. This
7 combination can be done in a variety of known ways.

8

9 It is noted that in the above example the difference between the transformation
10 used for the first and the second watermarks involves biasing the values of H and S.
11 Alternatively a wide variety of different changes could also be made. The key to
12 this fourth embodiment of the invention is that in effect a different transformation is
13 used for the first and the second watermarks.

14

15 While four embodiments of the invention have been shown herein, it should be
16 understood that many other characteristics and attributes of a digital watermark
17 could be used to practice the present invention in addition to the characteristics and
18 attributes described herein. Furthermore other known digital watermarking
19 techniques can be used together with and applied to the digital watermarks used for
20 the present invention. It is also noted that while in the above examples only two
21 watermarks were used, in some situations one could use three, four five or more
22 watermarks. That is, the embodiments of the invention specifically described herein
23 utilize two watermarks. It should be understood that any number of watermarks
24 could be utilized in like manner. Furthermore while the embodiments shown herein
25 utilize two separate watermarks, the two watermarks used to practice the present
26 invention could be combined into one watermark which has a plurality of separate
27 identifiable and measurable characteristics.

1

2 It is noted that while the present invention utilizes multiple watermarks with different
3 characteristics to differentiate original documents from copies of the original, one
4 can also utilize multiple watermarks with different characteristics for other reasons.
5 Documents may include multiple similar watermarks in addition to the watermarks
6 which have different characteristics according to the present invention. As used
7 herein, in general, the term "document" refers to a physical entity.

8

9 While the present invention has been described with respect to four specific
10 embodiments of the invention, it should be understood that various changes in
11 form and detail could be made without departing from the spirit and scope of the
12 invention. The scope of the present invention is limited only by the appended
13 claims.

1 I claim

2 1) A document which has embedded therein a first digital watermark having a first
3 set of characteristics and a second watermark having a set of characteristics which
4 differ from said first set of characteristics.

5

6 2) The document recited in claim 1 wherein said first watermark has a different
7 energy level from said second watermark.

8

9 3) The document recited in claim 1 wherein said first and second watermarks have
10 bit patterns and wherein the bit patterns which comprise said first watermark are
11 different from the bit patterns which comprise said second watermark

12

13 4) A method of creating a watermarked image which comprises the steps of:
14 modifying an HSI (hue, saturation, Intensity) representation of an image to imbed a
15 first watermark in said image and create a first watermarked image,
16 transforming said first watermarked image to the RGB (red, green, blue) color
17 space,
18 biasing the values which represent a second watermark toward a particular color,
19 modifying a said HSI values to imbed said biased second watermark in said
20 image and create a second watermarked image,
21 transforming said second watermarked image to the RGB color space, and
22 combining the values first and second watermarked images to create a final
23 watermarked image.

24

25 5) The method recited in claim 4 wherein said biasing is toward a particular color.

26

- 1 6) A method of differentiating copies of an original document from the original
2 document comprising, said document containing a first digital watermark which has
3 a first set of characteristics and a second digital watermark which has a second set
4 of characteristics,
5 reading said first and second watermarks from said original document and
6 comparing the resultant values to generate a first set of results,
7 reading said first and second watermarks from said copy of said original document
8 and comparing the resulting values to generate a second set of results, and
9 using differences between said first and second sets of results to differentiate an
10 original document from a copy of said original document.
11
- 12 7) The method recited in claim 6 wherein said first digital watermark has a first
13 energy level and said second watermark has a second energy level.
14
- 15 8) The method recited in claim 6 wherein said first watermark has a first bit pattern
16 and said second watermark has a different bit pattern.
17
- 18 9) The method recited in claim 6 where both said original document and said copy
19 have been subjected to wear.
20
- 21 10) The document recited in claim 1 wherein said second watermark was been
22 biased toward a particular color before it was inserted in said document.
23
- 24 11) A method of differentiating an original document from a copy of said document,
25 said document having first and second watermarks imbedded therein, comprising
26 the steps of comparing the characteristics of the said first and second watermarks in

1 said original document and comparing the characteristics of said first and second
2 watermarks in said copy.

3

4 12) the method recited in claim 11 wherein said first and second watermarks have
5 different grain structures.

6

7 13) The method recited in claim 11 wherein said first and second watermarks have
8 different intensity levels.

9

10 14) The method recited in claim 12 wherein said first and second watermarks have
11 different characteristics.

12

13 15) A document which contains an image which has embedded therein a plurality of
14 watermarks, each of said watermarks having characteristics which differ from each
15 other.

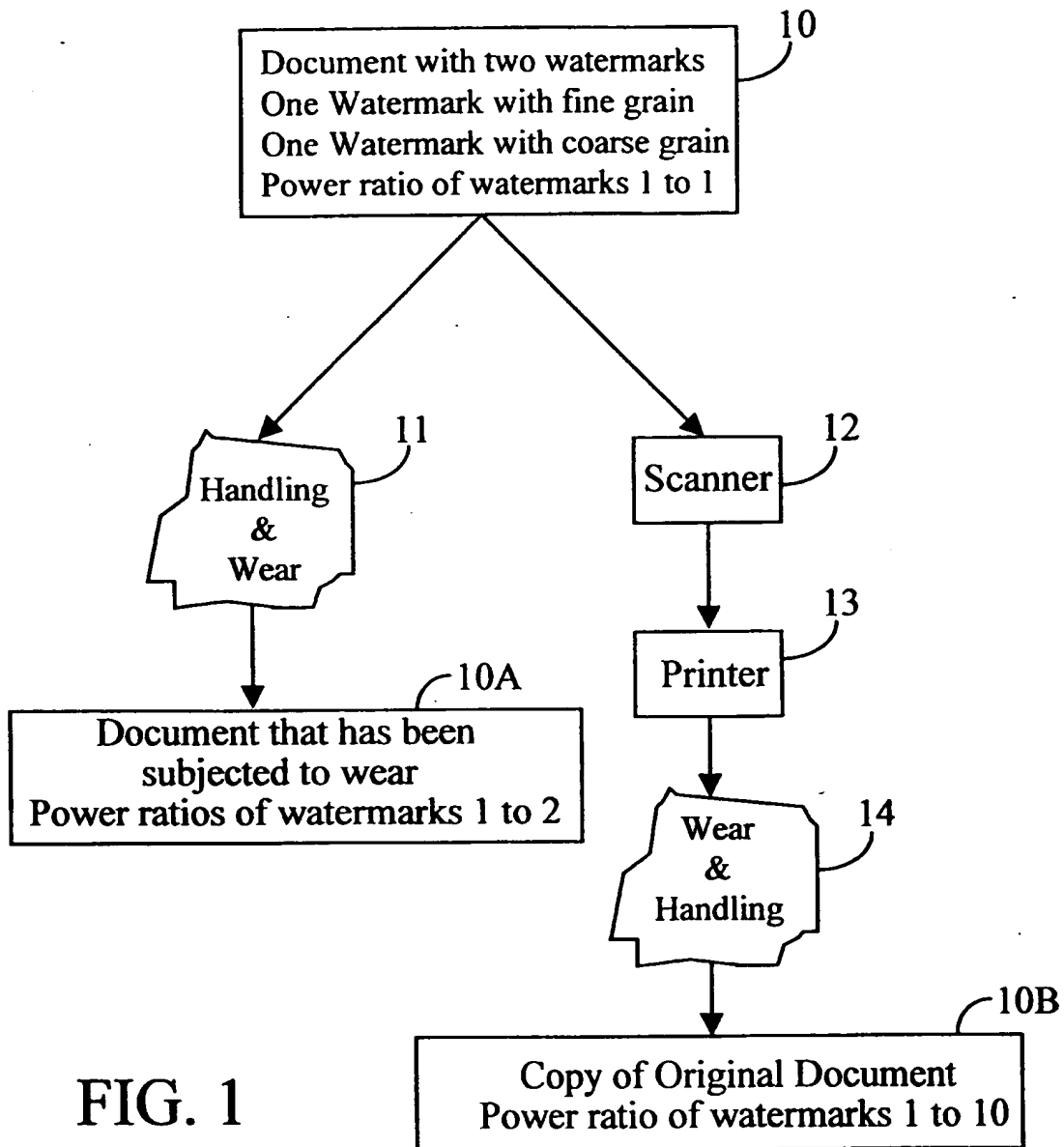


FIG. 1

FIG. 2A

Watermark with a fine grain (each block of pixels is 3 by 3)

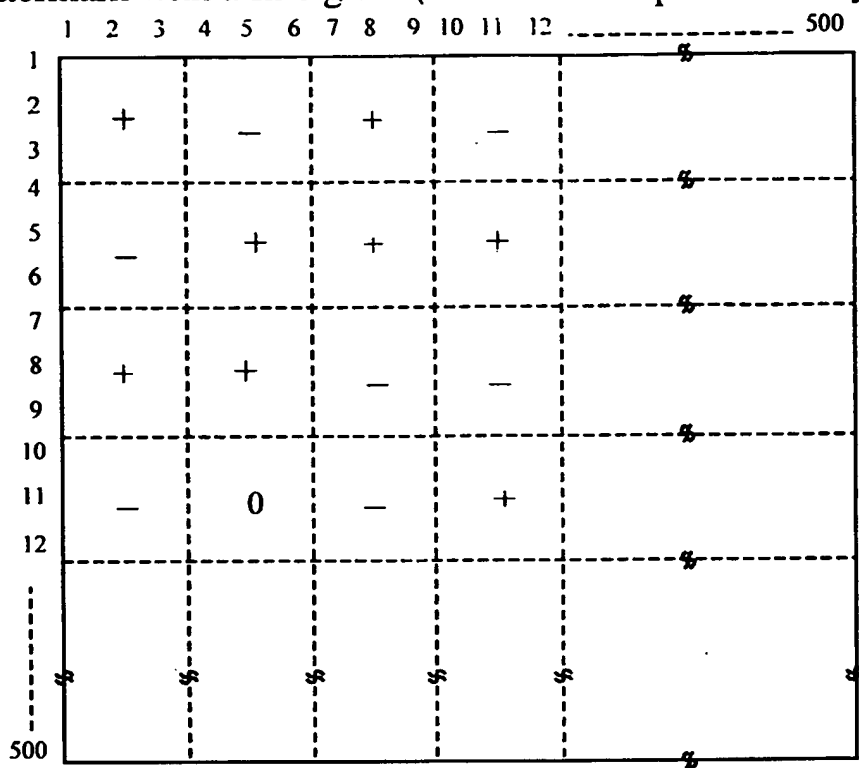


FIG. 2B

Watermark with a coarse grain (each block of pixels is 6 by 6)

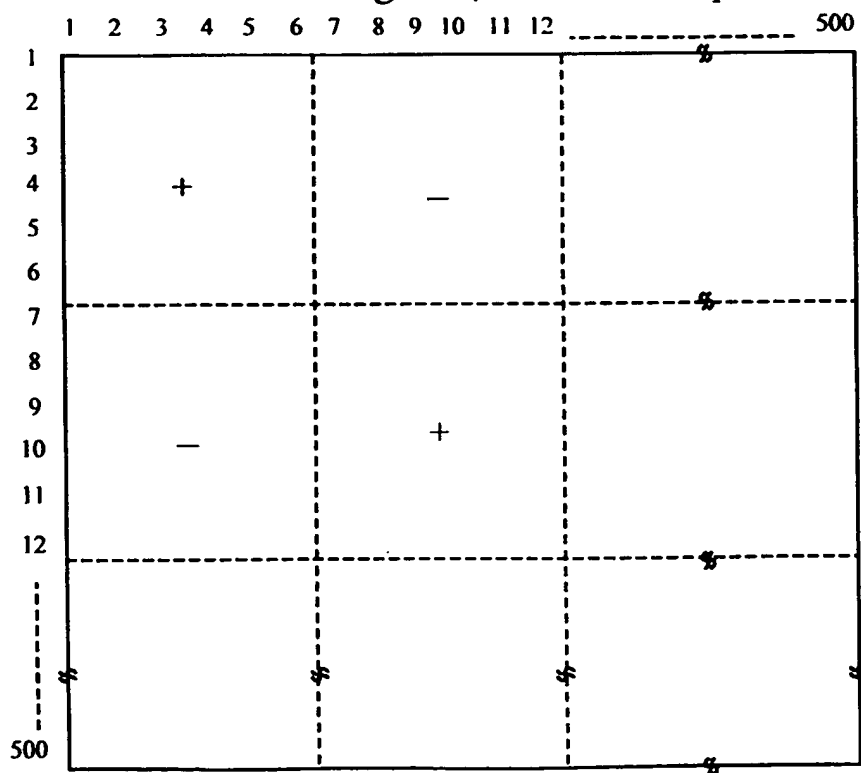
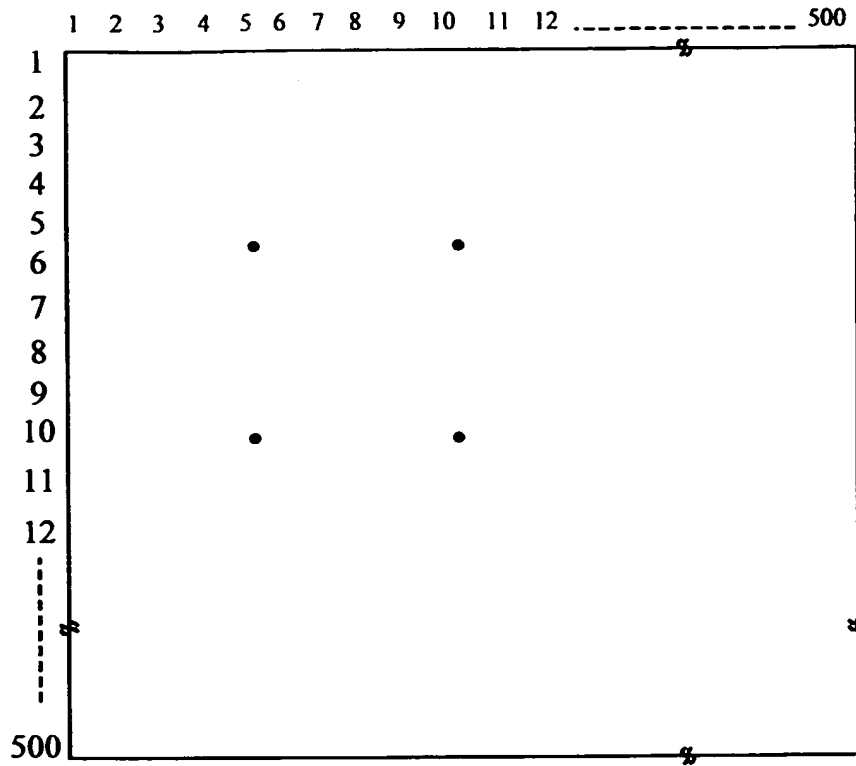
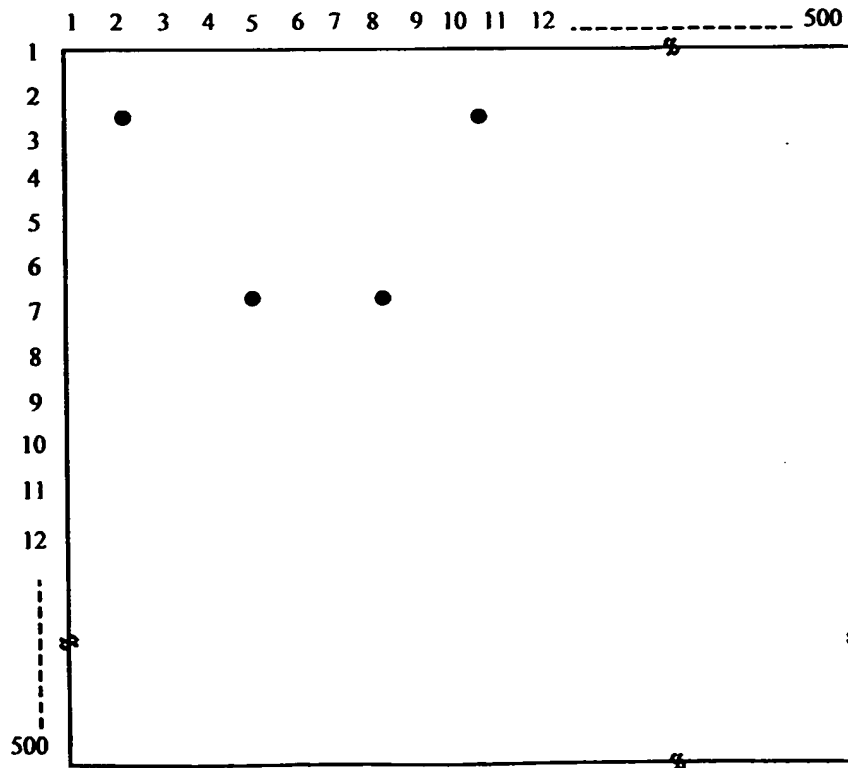


FIG. 3A Geometrically linear assignment of pixels to each bit**FIG. 3B** Geometrically random assignment of pixels to each bit

(1) $\text{RGB} \longrightarrow \text{HSI}$

(2) First Watermark

$\text{HSI} + \text{WM1}\Delta \xrightarrow{\text{T}} \text{RGB1}$

(3) Second Watermark

$\text{HSI} + \text{Biased WM2}\Delta \longrightarrow \text{RGB2}$

(4) Final image $(\text{RGB1} + \text{RGB2}) / 2 = \text{RGBF}$

FIG. 4